National Evaluation Series ${ }^{\text {TM }}$
The Advanced System for Educator Certification

## MATHEMATICS <br> (MIDDLE GRADES AND EARLY SECONDARY)

## Test Framework

|  | Content Domain | Range of <br> Competencies | Approximate <br> Percentage of <br> Test Score |
| ---: | :--- | :---: | :---: |
| I. | Mathematical Processes and <br> Number Sense | $0001-0003$ | $24 \%$ |
| II. | Patterns, Algebra, and Functions | $0004-0007$ | $28 \%$ |
| III. | Measurement and Geometry | $0008-0010$ | $24 \%$ |
| IV. | Statistics, Probability, and Discrete <br> Mathematics | $0011-0013$ | $24 \%$ |

## I. Mathematical Processes and Number Sense

## 0001 Understand mathematical problem solving.

- Identify an appropriate problem-solving strategy for a particular problem.
- Analyze the use of estimation in a variety of situations (e.g., rounding, area, plausibility).
- Solve mathematical and real-world problems involving integers, fractions, decimals, and percents.
- Solve mathematical and real-world problems involving ratios, proportions, and average rates of change.


## Understand mathematical communication, connections, and 0002 reasoning.

- Translate between representations (e.g., graphic, verbal, symbolic).
- Recognize connections between mathematical concepts.
- Analyze inductive and deductive reasoning.
- Apply principles of logic to solve problems.
- Demonstrate knowledge of the historical development of major mathematical concepts, including contributions from diverse cultures.


## 0003 Understand number theory.

- Analyze the group structure of the real numbers.
- Use complex numbers and their operations.
- Analyze the properties of numbers and operations.
- Apply the principles of basic number theory (e.g., prime factorization, greatest common factor, least common multiple).


## II. Patterns, Algebra, and Functions <br> 0004 Understand relations and functions. <br> - Demonstrate knowledge of relations and functions and their applications. <br> - Perform operations with functions, including compositions and inverses. <br> - Analyze characteristics of functions. <br> - Interpret different representations of functions.

0005 Understand linear, quadratic, and higher-order polynomial functions.

- Analyze the relationship between a linear, quadratic, or higher-order polynomial function and its graph.
- Solve linear and quadratic equations and inequalities using a variety of methods.
- Solve systems of linear equations or inequalities using a variety of methods.
- Solve higher-order polynomial equations and inequalities in one and two variables.
- Analyze the characteristics of linear, quadratic, and higher-order polynomial equations.
- Analyze real-world problems involving linear, quadratic, and higher-order polynomial functions.

0006 Understand exponential and logarithmic functions.

- Apply the laws of exponents and logarithms.
- Analyze the relationship between exponential and logarithmic functions.
- Analyze exponential and logarithmic functions and their graphs.
- Analyze real-world problems involving exponential and logarithmic functions.

Understand rational, radical, absolute value, and piece-wise defined 0007 functions.

- Manipulate rational, radical, and absolute value expressions, equations, and inequalities.
- Analyze the relationship between a rational, radical, absolute value, or piecewise defined function and its graph.
- Analyze rational, radical, absolute value, and piece-wise defined functions in terms of domain, range, and asymptotes.
- Analyze real-world problems involving rational, radical, absolute value, and piece-wise defined functions.


## III. Measurement and Geometry

0008 Understand measurement principles and procedures.

- Analyze the use of various units and unit conversions within the customary and metric systems.
- Apply the concepts of similarity, scale factors, and proportional reasoning to solve measurement problems.
- Analyze precision, error, and rounding in measurements and computed quantities.
- Apply the concepts of perimeter, circumference, area, surface area, and volume to solve real-world problems.

0009 Understand Euclidean geometry in two and three dimensions.

- Demonstrate knowledge of axiomatic systems and of the axioms of non-Euclidean geometries.
Use the properties of polygons and circles to solve problems.
- Apply the Pythagorean theorem and its converse.
- Analyze formal and informal geometric proofs, including the use of similarity and congruence.
- Use nets and cross sections to analyze three-dimensional figures.

0010 Understand coordinate and transformational geometry.

- Analyze two- and three-dimensional figures using coordinate systems.
- Apply concepts of distance, midpoint, and slope to classify figures and solve problems in the coordinate plane.
Analyze conic sections.
- Determine the effects of geometric transformations on the graph of a function or relation.
- Analyze transformations and symmetries of figures in the coordinate plane.


## IV. Statistics, Probability, and Discrete Mathematics

0011 Understand principles and techniques of statistics.

- Use appropriate formats for organizing and displaying data.
- Analyze data in a variety of representations.
- Analyze the use of measures of central tendency and variability.
- Analyze the effects of bias and sampling techniques.

0012 Understand principles and techniques of probability.

- Determine probabilities of simple and compound events and conditional probabilities.
Use counting principles to calculate probabilities.
- Use a variety of graphical representations to calculate probabilities.
- Select simulations that model real-world events.
- Analyze uniform, binomial, and normal probability distributions.

0013 Understand principles of discrete mathematics.

- Apply concepts of permutations and combinations to solve problems.
- Analyze sequences and series including limits and recursive definitions.
- Perform operations on matrices and vectors.

Apply set theory to solve problems.

